Long-Term Growth and Short-Term Volatility: The Labour Market Nexus*

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Abstract

We study the relationship between growth and variability in a DSGE model with nominal rigidities and growth driven by learning-by-doing. We show that this relationship may be positive or negative depending on the impulse source of fluctuations A key role is also played by the Frisch elasticity of labour supply and by institutional features of the labour market. Our general findings are that monetary shocks volatility will generally have a negative effect on growth, while the opposite tends to be true for fiscal and productivity shocks. These findings are somehow consistent with the existing empirical evidence: data show, in fact, a somewhat ambiguous relationship between output growth and real variability, but a generally negative relationship between output growth and nominal variability.

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1 Introduction

In macroeconomics growth and business cycles have been considered as two separate areas of research. In this paper we attempt to bridge these two areas by proposing a model of endogenous growth that gives a central position to uncertainty.

Until the 1980's macroeconomists regarded short-term economic fluctuations (or business cycles) as deviations around a smooth and stable trend growth path of GDP. Nelson and Plosser (1982) started a debate on the by now accepted fact that output does not show a strong tendency to return to trend after a shock: this fact questions the separation between growth and business cycles analysis. Indeed, the evidence on the persistence of the output process was interpreted by real business cycle theorists as a sign of the nature of the disturbances that caused business cycles, i.e. technological shocks. An alternative explanation to the high persistence of fluctuations comes from models where growth is endogenous: in fact, a generally neglected key implication of these models, which are often deterministic, is that any temporary disturbance that has an effect on the amount of growth-enhancing activities can produce permanent effects on the level of output.

Further evidence of a link between growth and cycles is provided by a number of empirical studies which report statistically significant correlations between output growth and output volatility using various cross-section and time series data. Following the seminal paper by Ramey and Ramey (1995), cross-country studies have consistently found that volatility exerts a significant negative impact on long-run (trend) growth, which is however stronger in poorer countries (see Martin and Rogers 2000, Kose et al. 2005, Hnatkovska and Loayza 2005). As to time series methods, using a univariate GARCH model on US data, Caporale and McKiernan (1998) find a positive effect, while Grier and Perry (2000) find no effect in a symmetric bivariate GARCH model of inflation and output growth, and Dawson and Stephenson (1997) reach the same conclusion from an examination of state level data.

Inflation and/or money average growth and volatility are generally found to negatively affect output growth using cross-section (e.g. Barro 1997 and 2001, Turnovsky and Chattopadhyay 2003), panel data (e.g. Andrés and Hernando 1997, Judson and Orphanides 1999), and time series methods (see Grier and Perry 2000 and Elder 2004). A careful examination of the problems of the different approaches is offered in the overview by Temple (2000). Finally, using multivariate GARCH models, Grier et al. (2004), Fountas et al. (2006) and Andreou et al. (2008) find a generally negative effect of the volatility of money shocks on output growth in G7 countries and a positive effect of growth volatility on output growth.

The existence of a relationship between growth and volatility has important policy implications as it suggests the possibility that policies designed to stabilize short-run fluctuations might also affect the long-run performance of the economy. Depending on whether this relationship is negative or positive, there is the presumption that successful stabilization would also entail either an improvement or deterioration in growth prospects. The potential significance of this is obvious, especially considering that it takes only small changes in the growth rate to produce substantial cumulative gains or losses in output.

It is therefore unsurprising that the relationship between growth and cycles is also receiving an increasing attention in the theoretical literature. In the so called 'schumpeterian' approach recessions have a positive impact on growth by reducing the opportunity cost of technological improvements. Aghion and Banerjee (2005) note that in this type of models the relationship between volatility and growth is likely to be positive. The relationship will become negative if credit constraints are pervasive, so that R&D has to be financed by current profits, a condition more relevant for developing countries. However this view is challenged by the empirical evidence on the procyclicality of R&D expenses (see Walde and Woitek 2004 and Barlevy 2007) in developed countries. In 'arrovian' models, where growth takes the form of learning-

¹A comprehensive overviews are in Gaggl and Steindl (2007) and in Aizenman and Pinto (2005) .

by-doing, revived by Romer (1986), recessions have a negative effect on growth (e.g. Blackburn 1999, Pelloni 1997 and Stadler 1990). Martin and Rogers (1997, 2000) and Blackburn and Galindev (2003) show that when knowledge (embodied or disembodied) accumulation externality works only through labour, volatility will be detrimental to growth. However, De Hek (1999), going back to Romer's (1986) specification of learning by doing, shows that volatility will have a positive effect on growth if the elasticity of the marginal utility of consumption is higher than one. Canton (2002) finds a positive relationship in a model where growth is driven by human capital accumulation and Jones et al. (2005) show that in a large class of convex models of endogenous growth, the relationship between growth and volatility is positive, even when preferences have less curvature than in the logarithmic case, with the magnitude of the effect being U-shaped with respect to the intertemporal elasticity of substitution.

These insights have been established within the context of purely real models of the economy with real shocks and real propagation mechanisms. Stochastic monetary models of endogenous growth are instead studied by Grinols and Turnovsky (1993) and Evans and Kenc (2003), who both derive a negative effect of money uncertainty, and Dotsey and Sarte (2000) and Varvarigos (2008), who find positive effects. Finally, in Turnovsky (2000) there's money superneutrality as regards both the rate and the variance of money growth.

While all these papers assume price flexibility, Blackburn and Pelloni (2004) and (2005) propose a model with technology \dot{a} la Romer (1986) where money enters the utility function and there is nominal wage-setting by unions. They analytically derive a negative relationship between growth and the volatility of nominal shocks and a positive relationship between growth and the volatility of shocks to the rate of subjective time discount.

In this paper we relax some of the most restrictive assumptions of these two models, i.e. those on leisure entering linearly in the utility function, on capital depreciating

fully in each period, and on the lack of persistence in the shocks hitting the economy. We show that, in fact, the Frisch (compensated) elasticity of labour supply (FELS), the rate of depreciation of capital and the degree of autocorrelation of exogenous disturbances are all important parameters in determining the effects of increased uncertainty.²

We consider both the case of a competitive labour market and of nominal wage setting, and include fiscal and technology shocks as well as monetary shocks. Finally, we consider the effects on inflation and its volatility, which could be useful to interpret the empirical findings summarised above.

In line with the existing literature, we assume a trend growth rate for money subject to stochastic shocks, while the ratio between public expenditure and consumption is constant and also subject to stochastic shocks. Of course many alternative assumptions could be introduced as regards the conduct of fiscal and monetary policies:³ we have chosen these hypotheses because they are best suited to understand some mechanisms connecting growth and volatility.

We find that with nominal rigidity monetary shocks volatility will generally have a negative effect on growth, which however becomes positive when the FELS is high and the rate of depreciation is less than 100%. In our benchmark calibration a higher volatility of the money growth rate, keeping its average constant, induces lower expected inflation and a higher variance of inflation and therefore a positive correlation between expected

²A parameter that measures the elasticity of total effort with respect to its return is found to influence the relationship between growth and volatility by Blackburn and Varvarigos (2008). However they use a very different model (e.g. the utility of leisure is a linear function of human capital, which is the only factor of production and which is produced by itself and public capital), thus our results bear little relationship to theirs.

³The setting of a fixed rate of increase for money was a popular approach to monetary policy in the 1970s and 1980s. In the past two decades central banks have shifted towards inflation targeting using the interest rate as an instrument. However, as stressed by Goodfriend (2002) there are several developments that may suggest a shift back from the interest rate to money aggregates as a policy instrument. First, progress in the payment system could make more difficult for a Central Bank to use just the short-term interest rate in the monetary transmission mechanism. Second, standard interest rate rules play no role when nominal interest rates hit the zero bound, as in the case of a liquidity trap.

growth and the variance of inflation. However, for lower values of the FELS, increased money volatility depresses growth and increases expected inflation, thus delivering a negative correlation between the two.

Uncertainty due to technology shocks leads to higher long-run growth and to higher inflation than in a deterministic environment. The effect on the first is lower and the second is higher the lower is the FELS.

The effect of fiscal shocks volatility on expected growth and inflation is positive with a high elasticity of labour supply, but becomes negative on the first and stronger on the second when the elasticity of labour supply is lower, or when, for a given level in the variance of the shocks, the serial correlation in the shocks is high enough.

No matter what shock we consider, a high rate of depreciation of capital dampens the effect of volatility on growth when it is positive and reinforces it when it is negative.

Finally, we show that the institutional features of the labour market are also important. Not only money shocks, and their variance, have real effects only with nominal wage setting, but the effect of technological variability is higher under nominal wage setting, while the volatility of the fiscal shock has larger effects on growth in a competitive labour market.

Coming to our solution techniques, it is common practice in macroeconomics to solve nonlinear dynamic stochastic systems using linear methods. However, these methods are not suitable to study the effects of the volatility of the exogenous shocks in complex dynamics environments, since by adopting a linear method all the second order effects will be wiped off. Until recently, this has constrained the literature jointly analysing business cycles and growth to the use of models that could be solved analytically. However some methodological contributions have appeared recently that allow researchers to circumvent this limitation. To evaluate the effects of the volatility of shocks on the endogenous variables of our model we use the perturbation method proposed by Schmitt-Grohé and Uribe (2004), which amounts to a second-order Taylor

approximation around a deterministic steady state.⁴ We conduct two types of sensitivity analysis: we vary some preference and technological parameters and consider alternative decompositions of the shock volatility between innovation variance and autocorrelation.

To better understand the interplay between the various effects at work, we first consider an analytically solvable special case, which is then used to interpret behaviorally the results we obtain numerically. In fact, our aim here is not to present a model rich enough, either in number of variables or in dynamics, to fit the data well or to be used for forecasting purposes, but rather to uncover new channels for the influence of volatility on growth not considered before in the literature and to elucidate whether there could be a conflict between long-run and short-run objectives, thus providing a conceptual basis for the formulation of optimal policies. This requires that the mapping between model structure and model implications is clearly understood.

The paper is organised as follows: section two describes the basic stochastic growth model incorporating exogenous monetary disturbances in the process governing money growth, technology and fiscal shocks; section three summarizes the general equilibrium conditions of the model, section four describes some preliminary analytical results, section five applies the perturbation method of Schmitt-Grohé and Uribe (2004) to evaluate the effects of volatility on growth. Section six concludes.

2 The Model

We consider an artificial economy in which there are constant populations (normalised to one) of identical, immortal households and identical, competitive firms. Time is discrete and indexed by $t = 0, 1...\infty$.

⁴Schmitt-Grohé and Uribe (2004) also provide Matlab codes to compute second-order approximations for any rational expectation model, whose equilibrium conditions can be written in a given form they describe. We are able to use these codes as the model we propose has the required form.

2.1 Firms

The representative firm combines N_t units of labour with K_t units of capital to produce Y_t units of output according to

$$Y_t = b_t (\overline{K}_t N_t)^{\alpha} K_t^{1-\alpha}, \quad \alpha \in (0,1)$$
(1)

$$b_t = C_b + \rho_b b_{t-1} + \varepsilon_{b,t}, \tag{2}$$

where C_b and ρ_b are constants. The shock $\varepsilon_{b,t}$ is assumed to be identically and independently distributed with mean zero, variance equal to $\sigma_{\varepsilon_b}^2$ and bounded support. The term \overline{K}_t represents an index of knowledge which is freely available to all firms and which is acquired through serendipitous learning-by-doing, as in the classic Romer (1986) paper. There is a vast empirical literature that documents the pervasive presence of learning-by-doing effects in the economy. Some recent evidence and references to other studies can be found in Thornton and Thompson (2001), Cooper and Johri (2002) and Jovanovic and Rousseau (2002).

Labour and capital are hired from households at the real wage rate $\frac{W_t}{P_t}$ and real rental rate R_t , respectively, where W_t is the nominal wage and P_t is the price of output. Profit maximisation implies that factors are paid at their marginal productivity:

$$\frac{W_t}{P_t} = \alpha b_t \overline{K}_t^{\alpha} N_t^{\alpha - 1} K_t^{1 - \alpha} = \alpha b_t N_t^{\alpha - 1} K_t, \tag{3}$$

$$R_t = b_t (1 - \alpha) \overline{K}_t^{\alpha} N_t^{\alpha} K_t^{-\alpha} - \delta = b_t (1 - \alpha) N_t^{\alpha} - \delta, \tag{4}$$

where δ is the depreciation rate and the second equalities in the expressions above are the result of a symmetry assumption for firms.

2.2 Households

The representative household derives lifetime utility, U, according to

$$U = \sum_{t=0}^{\infty} \beta^t \left[\log C_t + \mu \log \left(\frac{M_t}{P_t} \right) - \lambda L_t^{\eta} \right], \quad \beta \in (0, 1), \quad \lambda, \mu > 0, \ \eta > 1,$$
 (5)

where C_t denotes consumption, $\frac{M_t}{P_t}$ denotes real money balances and L_t denotes labour.

We choose a logarithmic specification for utility because it is suggested by recent estimates,⁵ and because it is consistent with additive separability in consumption and leisure. This separability makes it easier to clarify some of the mechanisms we are studying, i.e. the effect of the elasticity of labour supply, as will become clear in what follows. To generate a demand function for money, we adopt the familiar short-cut device of introducing money directly into the utility function, rather than specifying explicitly a separate transactions technology. The quantity M_{t-1} is understood to denote beginning-of-period t (i.e., end-of-period t-1) nominal cash balances which are augmented by a proportional monetary transfer, a_t .⁶ We assume that the disturbance is governed by the following process:

$$a_t = C_a + \rho_a a_{t-1} + \varepsilon_{a,t}. \tag{6}$$

The shock $\varepsilon_{a,t}$ is assumed to be identically and independently distributed with mean zero, variance equal to $\sigma_{\varepsilon_a}^2$ and bounded support. C_a is a constant, the scalar ρ_a is

⁵The literature on estimation of the IES uses a wide variety of models and data sets. Using the US aggregate consumption data, Hall (1988) found that expected interest rates had no effect on consumption growth. Attanasio and Weber (1993) showed evidence of aggregation bias in testing the Euler equation with aggregate data. Beaudry and van Wincoop (1996) also showed that aggregate data were uninformative in the point estimate of the IES and used a panel of state-level data to conclude that the IES estimate was probably close to one. More recently Vissing-Jørgensen and Attanasio (2003) and Mulligan (2004) results are roughly consistent with log utility specifications.

⁶In some models, it is end-of-period (rather than beginning-of-period) money holdings that serve as the reference point. To the extent that money yields utility by facilitating transactions, it seems more reasonable to adopt the present formulation. The assumption that monetary transfers are proportional (rather than lump-sum) is made largely for analytical convenience, as in other investigations (e.g., Bénassy 1995).

assumed to be less than one. Defining Z_t as real assets, the budget constraint for the household is given by

$$C_t + \frac{M_t}{P_t} + Z_{t+1} = \frac{W_t}{P_t} L_t + \frac{M_{t-1}a_t}{P_t} + (1 + R_t)Z_t - S_t, \tag{7}$$

where Z_t represents wealth and S_t is lump-sum taxation.

Each household confronts the problem of maximising the expected value of intertemporal utility in (5), subject to the sequence of budget constraints in (7) and initial conditions for Z_0 and M_0 . The information set conditioning expectations consists of the values of all parameters, the current and past values of all variables and the probability distributions of all shocks. The problem is solved, in part, by choosing plans for consumption, money balances and asset holdings that satisfy the following conditions:

$$C_t^{-1} = \beta E_t C_{t+1}^{-1} (1 + R_{t+1}), \tag{8}$$

and

$$\frac{\mu}{M_t} = \frac{1}{C_t P_t} - E_t \beta \frac{\gamma a_{t+1}}{C_{t+1} P_{t+1}}.$$
(9)

Using the transversality condition $\lim_{\tau\to\infty} \beta^{\tau} E_t\left(\frac{M_{t+\tau-1}a_{t+\tau}}{P_{t+\tau}C_{t+\tau}}\right) = 0$, equation (9) can be solved forward to give:

$$\frac{M_t}{C_t P_t} = \mu (1 - \beta)^{-1}. (10)$$

We consider two alternative scenarios for the labour market. In the first scenario, the labour market is characterised by monopolistic unions. Bewley's (1999) detailed study of firms' wage policies based on interviews with managers finds ample evidence of downward nominal wage rigidities. More recently, the multi-country study of Dickens et al. (2007) uncovers evidence of significant downward nominal and real wage rigidities in most of the countries in their sample. We assume that wage setting takes place prior to the realisations of shocks, on the basis of one-period contracts. In this case,

therefore, the economy displays nominal rigidities, as in the early contracting models of Gray (1976) and Fischer (1977), as well as those of a more recent vintage (e.g., Bénassy 1995). The nominal wage is fixed at the level that maximizes households' expected utility, taking into account the constraint given by labour demand. The optimality condition for the nominal wage is found to be:

$$\eta \lambda E_{t-1} L_t^{\eta} = \alpha W_t E_{t-1} L_t (P_t C_t)^{-1}. \tag{11}$$

Hence in equilibrium the marginal expected benefit of working is equal to the expected cost. In the second scenario, the labour market is perfectly competitive. Labour supply turns out to be:

$$\frac{W_t}{P_t}C_t^{-1} = \eta \lambda L_t^{\eta - 1},\tag{12}$$

From (12) we can see that the Frish elasticity (FELS) is equal to $1/(\eta-1)$. Households' equilibrium is now characterised completely by the first-order conditions in (8) and (10), the optimal condition for the nominal wage (11) or for labour supply (12), the budget constraint in (7), the initial conditions for money holdings and financial wealth and the transversality condition:

$$\lim_{\tau \to \infty} \beta^{\tau} E_t \left(\frac{Z_{t+\tau+1}}{C_{t+\tau}} \right) = 0. \tag{13}$$

3 General Equilibrium

The solution of the model is computed by combining the equilibrium conditions for households listed above, with the profit maximization condition for firms (3) and (4), the market clearing conditions for capital, $K_t = Z_t$, for labour, $N_t = L_t$, for goods, $C_t + K_{t+1} + G_t = Y_t + (1 - \delta)K_t$, where G_t denotes government spending in period t,

and for the money market. Money supply, H_t , moves in conformance with:

$$H_t = a_t H_{t-1}. (14)$$

The equilibrium condition for the money market is then $M_t = H_t$.

We assume that the government runs a continuously balanced budget, so that $G_t = S_t$. Government expenditure is assumed to evolve according to:

$$G_t = u_t C_t, (15)$$

$$u_t = C_u + \rho_u u_{t-1} + \varepsilon_{u,t}. \tag{16}$$

The shock $\varepsilon_{u,t}$ is assumed to be identically and independently distributed with mean zero, variance equal to $\sigma_{\varepsilon_u}^2$ and bounded support, C_u is a constant and the scalar ρ_u is assumed to be less than one.⁷

The labour market equilibrium condition with nominal wage setting can be rewritten as (derivation in the Appendix):

$$L_{t} = \left(\frac{\alpha^{2} a_{t} b_{t} K_{t} E_{t-1} L_{t} a_{t}^{-1}}{\eta \lambda C_{t} E_{t-1} L_{t}^{\eta}}\right)^{1/(1-\alpha)}.$$
(17)

When the labour market is competitive, its equilibrium condition, obtained just by equating labor demand (3) and labour supply (12) is:

$$L_t = \left(\frac{\alpha b_t K_t}{\eta \lambda C_t}\right)^{1/(\eta - \alpha)}.$$
 (18)

⁷The simplifying assumption made regarding the government budget financing is that all transfers are fully financed by money creation, while all government spending is exclusively financed by lump-sum taxation. In this way we rule out the possibility of an accommodative monetary policy and we manage to study the effects of the volatilities of public expenditure and of money supply separately.

4 Some Analytical Results

To pin down some of the mechanisms relating growth and uncertainty, in this section we consider a set of very restrictive assumptions under which the model admits a closed form solution. The findings in this section will be useful in interpreting the results we get by simulation in the extended model.

When $\delta = 1$ and the fiscal shock u_t is i.i.d., the following relationship, derived in the Appendix, holds:

$$\frac{K_{t+1}}{Y_t} = \frac{\varkappa(1+u)}{(1-\varkappa)(1+u_t) + \varkappa(1+u)}.$$
 (19)

and where $\varkappa \equiv (1 - \alpha)\beta$, and $u \equiv E_t u_{t+i}$ for $i = 1, 2..\infty$. This implies that the rate of investment is a decreasing and convex function of the fiscal shocks and therefore will increase on average when the variance of the shocks increases, by Jensen's inequality. We shall label this the 'precautionary saving effect', as it captures the fact that, in the face of increased uncertainty agents react by reducing current consumption, thus raising the pace of growth.

4.1 Money Wage Setting

Consider the nominal wage setting scenario. Assume that $\eta = 1$, and that all shocks are i.i.d and uncorrelated. We can then derive (see the Appendix):

$$L_t = \frac{\alpha^2 a_t \left[(1 - \varkappa)(1 + u_t) + \varkappa(1 + u) \right]}{a\lambda(1 - \varkappa)}.$$
 (20)

where $a \equiv Ea_{t+i}$ for $i = 1, 2...\infty$. Labour is an increasing linear function of the fiscal and the money shock. In fact both shocks cause an increase in aggregate demand and therefore in labour demand.

We can now state the following:

Proposition 1 Assume $\delta = 100\%$, all shocks are i.i.d. and uncorrelated with each other and η is equal to one. Then the following expression for the growth rate of consumption in the presence of money wage setting holds:

$$\frac{C_{t+1}}{C_t} - 1 = b_{t+1} \varkappa (1+u) \frac{\left(\frac{\alpha^2 a_{t+1}[(1-\varkappa)(1+u_{t+1})+\varkappa(1+u)]}{a\lambda(1-\varkappa)}\right)^{\alpha}}{(1-\varkappa)(1+u_{t+1})+\varkappa(1+u)} - 1.$$
 (21)

Proof. See Appendix. ■

As we have seen, given the assumed specifications of preferences and technology, the TFP shock has no effect on the marginal choice between leisure and consumption or on the time path of consumption. Growth is then a linear function of the technology shock b_{t+1} , through a direct effect on the production function. This means that the variance of this shock will not affect average growth. Growth is instead a strictly concave function of the monetary shock, so its variance will have a negative effect on average growth. The fraction raised to the power α in (21) is just L_{t+1} . Even if expected labour is not affected by σ_a^2 , since, as shown by (20), labour is a linear function of the money shock, however, because of the diminishing marginal productivity of labour, i.e. since $\alpha < 1$, the expected rate of growth will be affected by σ_a^2 . We could label this the 'diminishing returns to labour' effect. The effects of a mean-preserving spread in the distribution of the fiscal shocks can also be read from (21): u_{t+1} appears twice in (21). A first time it appears because it impinges on income through equilibrium employment, i.e. again through a 'diminishing returns to labour' effect; u_{t+1} also influences the propensity to save, as can be seen from (19): we have labeled this the 'precautionary saving effect'. The combination of these two effects makes the rate of growth at time t+1 a convex function of u_{t+1} . Calculating a second-order approximation of the rate of consumption growth as in (21) and taking expectations we get:

$$E\frac{C_{t+1}}{C_t} - 1 \simeq A - 1 + A_a \sigma_a^2 + A_u \sigma_u^2, \tag{22}$$

with
$$A \equiv b\varkappa \left(\frac{\alpha^2(1+u)}{(1-\varkappa)\lambda}\right)^{\alpha}$$
, $A_a \equiv \frac{A\alpha(\alpha-1)a^{-2}}{2} < 0$, $A_u \equiv \frac{A}{2}(\alpha-2)(\alpha-1)(1-\varkappa)^2(1+u)^{-2} > 0$.

In words, an increase in σ_u^2 causes an increase in precautionary savings which more than offsets the 'diminishing returns to labour effect': the net effect on expected growth is positive.

4.2 Competitive Labour Market

When the labour market is competitive equilibrium employment is given by (the derivation is in the Appendix):

$$L_t = \left(\frac{\alpha \left[(1 - \varkappa)(1 + u_t) + \varkappa(1 + u) \right]}{\eta \lambda (1 - \varkappa)}\right)^{1/\eta}.$$
 (23)

By comparing (20) and (23) we see that employment will be higher than in the presence of unions, i.e. when labour is supplied monopolistically. Labour is an increasing and concave function of u_t . The curvature of the function is stronger the lower the Frisch elasticity of labour supply (the higher is η). A mean-preserving spread in the distributions of the fiscal shock will induce employment to decrease on average. The effects of volatility on expected labour are referred in the rest of the paper as 'employment effects'. We are now ready for:

Proposition 2 Assume $\delta = 100\%$ and all shocks are i.i.d. and uncorrelated. Then the following expression for the rate of growth of consumption holds if the labour market is competitive:

$$\frac{C_{t+1}}{C_t} - 1 = \frac{b_{t+1} \left(\frac{\alpha[(1-\varkappa)(1+u_{t+1})+\varkappa(1+u)]}{(1-\varkappa)\eta\lambda} \right)^{\alpha/\eta}}{\left(1 + \frac{(1+u_{t+1})(1-\varkappa)}{\varkappa(1+u)} \right)}$$
(24)

Proof. See Appendix. ■

As in the previous case, growth is a linear function of the technology shock b_{t+1} , so the variance of this shock will not affect unconditional average growth. The fiscal

shocks enter (24) in a fashion analogous to that in which they enter (21), so we expect the effects of an increase in σ_u^2 to be similar to those we have seen in the economy with unions. In fact we have the following approximation:

$$E\frac{C_{t+1}}{C_t} - 1 \simeq B - 1 + B_u \sigma_u^2, \tag{25}$$

with
$$B \equiv b \varkappa \left(\frac{\alpha(1+u)}{(1-\varkappa)\eta\lambda}\right)^{\alpha/\eta}$$
, $B_u \equiv \frac{B}{2} \left(\frac{1-\varkappa}{1+u}\right)^2 \left[\left(\frac{\alpha}{\eta}-1\right)\left(\frac{\alpha}{\eta}-2\right)\right] > 0$.

Intuitively, as in the previous case, an increase in σ_u^2 causes an increase in precautionary savings which more than offsets the negative 'employment' and 'diminishing returns to labour' effects. The higher is η the lower the positive effect of volatility as the negative 'employment effect' gets stronger. We can also notice that expected growth will be higher than when labour is sold monopolistically (by comparing A and B with $\eta = 1$) and that the positive effect of volatility on growth will be higher as well (by comparing A_u and B_u with $\eta = 1$).

5 Simulating the Model

In order to study the effects of volatility of the exogenous shocks on growth in the general case, the model is solved following the numerical method based on accurate second-order approximation to the policy functions around the deterministic steady state devised by Schmitt-Grohé and Uribe (2004).⁸ This method amounts to a pure perturbation approach in which the solution to the model is such that the coefficients on the terms linear and quadratic in the state variables in the second-order Taylor expansion of the decision rule are independent of the volatility of the exogenous shocks.

⁸Kim et al. (2008) propose an alternative algorithm for calculating second order approximations to the solutions to nonlinear stochastic rational expectation models based on the "state free" approach described in Sims (2001). More recently Lombardo and Sutherland (2007) have proposed a methodology for computing second-order accurate solutions of non-linear rational expectation models using a two-step algorithm devised for the solution of linear expectation models. Their algorithm generates identical results to those reported by Schmitt-Grohé and Uribe (2004) in their example on a stochastic growth model.

This implies that the presence of uncertainty affects the solution to the model only via a constant term.⁹

5.1 Inducing Stationarity

In this economy a number of variables, such as output, consumption etc. will not be stationary along the balanced-growth path. We therefore perform a change of variables, so as to obtain a set of equilibrium conditions that involve only stationary variables. We note that non stationary variables at time t are cointegrated with K_t , while the same variables at time t+1 are cointegrated with K_{t+1} . We divide variables by the appropriate cointegrating factor and denote the corresponding stationary variables with lowercase letters.

Using (15), the economy wide resource constraint can be written as:

$$1 + g_{t+1} = \frac{c_{t+1}}{c_t} \left[b_t L_t^{\alpha} - c_t (1 + u_t) + 1 - \delta \right]. \tag{26}$$

where $c_t \equiv \frac{C_t}{K_t}$ and $g_{t+1} = \frac{C_{t+1}}{C_t} - 1$ i.e. g_t indicates consumption growth.

Using (4) and (9), the Euler equation becomes:

$$1 = E_t \frac{\beta \left[(1 - \alpha) b_{t+1} L_{t+1}^{\alpha} + (1 - \delta) \right]}{1 + q_{t+1}}.$$
 (27)

Equation (10) can be written as:

$$m_{p,t} = \frac{\mu c_t}{1 - \beta}. (28)$$

where $m_{pt} \equiv \frac{M_t}{P_t K_t}$.

⁹By contrast, in the method devised by Collard and Juillard (2001) the second-order Taylor expansion is computed around the means of the distribution implying that the coefficients of the the approximated solutions depend on the level of uncertainty.

Equation (10) also tells us that inflation $\pi_{t+1} = \frac{P_{t+1}}{P_t} - 1$ evolves according to:

$$(1+\pi_t)(1+g_t) = a_t. (29)$$

Coming to the labour market equilibrium, (17) in terms of stationary variables becomes:

$$L_{t} = \left(\frac{\alpha^{2} a_{t} b_{t} E_{t-1} L_{t} a_{t}^{-1}}{\eta \lambda c_{t} E_{t-1} L_{t}^{\eta}}\right)^{1/(1-\alpha)},$$
(30)

and (18) becomes:

$$L_t = \left(\frac{\alpha b_t}{\eta \lambda c_t}\right)^{1/(\eta - \alpha)}.$$
 (31)

A stationary competitive equilibrium is a set of stationary processes $\{c_t, g_t, m_{pt}, \pi_t, L_t\}$ satisfying (26), (27), (28), (29), and (30) (in case of monopolistic wage setting) or (31) (if the labour market is competitive), given the exogenous stochastic processes $\{a_t, b_t, u_t\}$ and the transversality conditions:

$$\lim_{\tau \to \infty} \beta^{\tau} E_t \left(\frac{m_{t+\tau}}{c_{t+\tau}} \right) = \lim_{\tau \to \infty} \beta^{\tau} E_t \left(\frac{z_{t+\tau+1}}{c_{t+\tau}} \right) \left(b_t L_{t+\tau}^{\alpha} - c_{t+\tau} (1 + u_{t+\tau}) + 1 - \delta \right) = 0.$$

5.2 Deterministic Balanced Growth Path

We have now to pin down the deterministic balanced growth path equilibrium, which will be the centre of our approximation. To indicate steady-state variables we drop the time subscript, i.e. x is the steady state value of the generic variable x_t . We have the following steady-state relationships:

$$1 + g = bL^{\alpha} - c(1+u) + 1 - \delta, \tag{32}$$

$$m_p = \frac{\mu c}{1 - \beta},\tag{33}$$

$$1 + g = \beta \left[(1 - \alpha)bL^{\alpha} + 1 - \delta \right], \tag{34}$$

$$(1+\pi)(1+g) = a, (35)$$

$$L = \left(\frac{b\alpha^2}{\eta \lambda c}\right)^{1/(\eta - \alpha)}.$$
 (36)

If the labour market is competitive instead of (36) we have

$$L = \left(\frac{b\alpha}{\eta \lambda c}\right)^{1/(\eta - \alpha)}.$$
 (37)

Finally, from (2), (6) and (16):

$$C_b = (1 - \rho_b)b, \tag{38}$$

$$C_a = (1 - \rho_a)a,\tag{39}$$

$$C_u = (1 - \rho_u)u. \tag{40}$$

We will study the implications of higher uncertainty on growth considering first the case of monopolistic nominal wage setting, and then the case of a competitive labour market.

5.3 Calibration

To implement the simulation method we have to choose values for the parameters appearing in the equations. The time period in the model is assumed to be one year. For some of these parameters, estimates are available in the empirical literature, others are chosen in order to make the steady-state values of the variables consistent with the data of the US economy. For each parameter we choose a benchmark value. To check for the robustness of our results we then consider a range of other possible values for some of the parameters, fixing the other parameters at their benchmark level.

The baseline calibration of the model is reported in Table 1, where most of benchmark parameter values are set along the lines of the existing literature. Consistently

with Schmitt-Grohé and Uribe (2007) the subjective discount factor β equals 0.96, the annual rate of depreciation of capital δ equals 0.1 and the cost share of labour α is set to 0.7. We set η at 2.5, while μ and λ are implied values.

The persistence of the money supply shock and the annual standard deviation of the innovation have been estimated over the period 1980-2007 using FRED data for seasonally adjusted M2. As in Schmitt-Grohé and Uribe (2007) the autoregressive parameters in the driving forces b_t and u_t are set equal to 0.85 and 0.87, respectively, while the standard deviations of the innovations are $\sigma_{\varepsilon_b} = 0.0212$ and $\sigma_{\varepsilon_u} = 0.0102$.

As in Galí et al. (2007) we set the share of government purchases in value added to be 20 percent in steady state, which is in line with the observed U.S. postwar average. In the U.S. M2 was on average about 52 percent of annual GDP over the period 1980 to 2007. King and Rebelo (1999) suggest that the average GDP-capital ratio in the U.S. is about 50% on annual basis. This gives steady-state values for m_p and s equal to 0.26 and 0.1, respectively. The steady-state inflation rate is assumed to be 4 percent per year. This value is consistent with the average U.S. consumer price index change over the period 1980-2007. The steady-state value for L is 0.2. Following Jones et al. (2005) the value for the non-stochastic growth rate of consumption is set to 2%.

5.4 Volatility and Growth under Nominal Wage Setting

We first consider the effects of nominal and real volatility on growth under the assumption that the nominal wage is set by a monopolistic union prior to the realisations of shocks. In this case monetary shocks and their variance have real effects.

Tables 2-4 report the effects of the volatility of the exogenous shocks on the unconditional means of consumption growth, E(g), of labour E(L) and inflation $E(\pi)$, and on the respective standard deviations, σ_g , σ_L and σ_{π} . We also report the standard deviations of each relevant shock, σ_a , σ_b , σ_u in turn.

The first row of each table displays the results obtained by using benchmark values

for the parameters of Table 1. To check for the robustness of our findings we study the sensitivity of our results using alternative values for the standard deviation of the innovation, holding all other parameters fixed. Then we vary the persistence of each shock, holding all other parameters at their benchmark values. We also check how expected growth changes when shocks' serial correlation changes, while their variance is fixed. Finally, we vary the labour supply coefficient η , the subjective discount factor β , the rate of capital depreciation δ and the steady-state employment level L.

5.4.1 Monetary Shocks Volatility

Table 2 shows that, in many cases, increased monetary policy variability results in lower growth and a lower level of equilibrium employment. First we notice that, given equation (27) and abstracting from the real shocks, up to a first order the rate of growth goes up if labour goes up as well. This is because the rate of return on capital is an increasing function of labour. So we first focus on this latter variable to interpret this result. In particular, the employment rate will be lower the higher is η . Our intuitive explanation is built around the optimal condition for the nominal wage (11). We can see that for given price level and consumption, the wage is the ratio of the expected value of a convex function of employment and of the expected value of a linear function of employment. So for a given level of employment, if the variance of employment increases, then the numerator will increase more than the denominator, pushing up the target real wage, or in other terms, through labour demand, pushing down equilibrium employment. So we have a 'target real wage effect', involving a negative 'employment effect'. Notice however that, by (3), labour demand is a convex function of the real wage, so that an increase in the variability of the real wage tends, through this mechanism, to increase employment. This is the 'labour demand effect'.

The sign of the relationship between nominal volatility and consumption growth tends to be positive for low values of the coefficient η . Intuitively, the lower is η the

weaker the 'target real wage effect' and the implied 'employment effect', as Table 2 shows. The sum of the positive 'precautionary saving effect' and 'labour demand effect' then prevails. Looking again at (27) from a different angle, we have to consider that the expression on the right hand side is concave in labour (as the rate of return of capital is concave in labour, this is the 'diminishing returns to labour effect') and convex in growth, so an increase in the variance of labour moves the expression down and an increase in the variance of growth moves it up, making it possible for labour and growth to move in opposite directions with increased uncertainty (in Table 2 this is seen to happen for $\eta = 1.5$). In other words since the rate of return of capital is a concave function of labour, it is possible that the expected return of capital goes down when labour stays constant or even increases slightly on average, while becoming more volatile. This pushes growth down.

Conversely, the higher η , the larger in absolute value are the negative effects produced by monetary volatility on the unconditional mean of consumption growth. In fact, the lower the FELS, the higher the positive response of the nominal wage to the variance of the monetary shock i.e. the 'target real wage effect', and, as a consequence, the stronger the negative 'employment' effect on the rate of return of capital, which dominates the positive 'precautionary saving effect' and 'labour demand effect'. Thus, contrary to the results obtained in the analytical model, increased nominal uncertainty could either increase or decrease expected growth rates.

We notice that higher persistence of the monetary shock implies a lower effect on expected growth. This is explained by the fact that in the model only money surprises have real effects. If the model had featured, for instance, staggered wage contracts, monetary shocks would have had more persistent effects and money shocks volatility would have had larger effects on growth volatility: including such mechanisms in the model is a direction for future research. Table 2 also reports the set of statistics when the depreciation rate of capital δ varies: a higher δ is associated with lower expected

rates of growth. This will be seen to happen to be true for all sources of fluctuations.

Coming to inflation, we first note that a higher trend inflation π diminishes the negative effect on expected growth due to nominal volatility. We suggest this is a consequence of a lower 'target real wage effect': for a given variance of money growth, an increase in average money growth leads to higher output growth, because it means an improvement in the information available to agents when they choose the nominal wage and a reduction in the related distortion.

Consider now the effects of nominal uncertainty on inflation. We observe that an increasing volatility of the money growth rate, keeping its average constant, brings about lower mean inflation and a higher standard deviation of inflation. In such circumstances, in the long run, we expect a positive correlation between growth and inflation and a negative correlation between growth and the variance of inflation, when η is higher than 1.5, as growth is pushed down along inflation. On the other hand, for decreasing values of the FELS, money uncertainty reduces growth and increases mean inflation, giving rise to a negative correlation between the two.

5.4.2 Technological Shocks Volatility

Table 3 shows that in the presence of technological variability uncertainty increases average consumption growth. This is due to the 'precautionary saving' effect. However, the largest impact of uncertainty upon growth is observed for low levels of the parameter η : when η is high the 'target real wage effect' tends to the dampen the 'precautionary saving' effect.

We also observe that changes in the variability of the innovation, σ_{ε_b} , have a larger impact on the unconditional mean of growth rates than changes in the persistence of the shock, ρ_b . Table 3 also shows how expected growth changes when the autocorrelation coefficient in the exogenous state variable changes, while keeping its variance fixed. We notice that even if technological uncertainty in itself increases growth, how-

ever a negative correlation between growth and its variance may be detected in the data (in our example this happens when increasing ρ_b from 0.3 to 0.4). This shows that it could be important in empirical analysis to decompose total variability into a pure 'risk' element, due to the innovation variance, and the increase in persistence, which is a predictable element, a point raised in Wolf (2005).

Turning to the effects on inflation, we observe that increasing uncertainty gives rise to high mean inflation and high inflation volatility. Contrary to what has been seen in the case of nominal volatility, here the relationship between expected growth and mean inflation is positive. However, this relationship is sensitive to the level of the FELS. Actually, a lower FELS reduces the expected growth of consumption, but increases the expected inflation rate.

5.4.3 Fiscal Shocks Volatility

The interplay between the various effects of uncertainty, i.e the positive ones (through precautionary savings and the convexity of labor demand with respect to the real wage) and the negative one (through the higher target real wage) is particularly difficult to disentangle in the case of fiscal shocks. Table 4 shows that consumption growth increases as fiscal variability rises if the FELS is sufficiently high, and if the coefficient of autocorrelation of fiscal shocks is lower than 0.95. However, in all cases we observe that the effects are negligible. We also notice that varying the serial correlation of the fiscal shock has a non-linear effect on average growth rate: we observe first a positive, then a negative relationship. Similarly, even for a high FELS ($\eta = 2.5$), fixing the variance of the shock at its benchmark value, if the autocorrelation of the shocks is above 0.6, expected growth will be decreasing in ρ_u . So contrary to what happens in the analytically solvable case, increased fiscal spending uncertainty is shown to either increase or decrease expected growth rates.

The effect of fiscal shocks volatility on mean inflation and its variance is positive

and becomes stronger for a low FELS. Clearly, the sign of the relationship between expected growth and expected inflation is sensitive to the persistence of the fiscal shock, either for given or changing variance of the shock.

5.4.4 The Effect of the Frisch Elasticity of Labour

From the above results it clearly emerges that the size of the Frisch (compensated) elasticity of labour supply is a crucial parameter in determining the effects of real and nominal volatility. We recall that available estimates from micro data vary widely, due to measurement errors and sample selection bias problems, but most surveys report a "consensus" estimate for labour supply elasticity of -0.1 for males, with the income effect being the double in absolute value of the substitution effect. Blundell and Macurdy (1999) and Borjas (2008) offer recent overviews of the literature. This would correspond to a value for η equal to 11. The elasticity of labour supply for females is estimated to be higher (see for instance Blau and Kahn, 2007). Aggregate models often assume elastic labor supply, despite the low estimates from empirical studies based on individual data. The explanation offered is that fluctuations of hours are mainly accounted for by participation rates, so that the important margin is the extensive rather than the intensive (see, for instance, Rogerson and Wallenius 2009 and Chang and Kim 2006). Given the ongoing debate on the issue, we offer results on a wide range of values of the FELS. Figures 1-3 plot the relationship between the unconditional means of consumption growth, E(q), labour E(L) and consumptioncapital ratio E(c) and the standard deviation of each shock, for four different levels of the parameter η . In particular, in each plot we vary the standard deviation of the innovation, holding the serial correlation and all other parameters fixed at their benchmark levels.

For high values of the parameter η we observe that uncertainty has a negative effect on growth in the case of money and fiscal shocks, while the positive effect is lowered by a high value of η in the case of the technology shock.

5.5 Volatility and Growth in a Competitive Labour Market

Consider now the effects of uncertainty on average growth under competitive labour markets with flexible wages. Tables 5-6 present the effects of the volatility of the real shocks on the unconditional mean of consumption growth, E(g), on mean employment, E(L) and on mean inflation $E(\pi)$.

Close inspection of the results reveals that in general the sign of the relationship between the volatility of the shocks and average growth is not affected by the labour market wage setting mechanism, however the magnitude of the observed effects may change considerably.

Table 5 shows that the effects of uncertainty of the technology shock are still positive with a competitive labour market, but the size of the effects is systematically lower than in a monopolistic market with nominal rigidities. Unsurprisingly the role played by labour market institutions in affecting the relationship between growth and volatility tends to be higher, the lower the FELS. Furthermore, when we vary the persistence of the technology shock, ρ_b , holding σ_b and all other parameters fixed, we observe a non-linearity, with expected growth and its volatility being negatively related for $\rho_b > 0.7$. A higher rate of physical capital depreciation has a negative effect on growth for a given technological variability. Finally, for a given level of the FELS, we observe a positive correlation between the mean value of growth and expected inflation, as well as a positive correlation between expected growth and inflation volatility.

Larger positive effects are instead observed under a competitive labour market when the source of economic fluctuation is given by fiscal policy (see Table 6): this confirms the result we found in the analytical setting. As seen in the case of nominal wage rigidities, expected growth is lower than in a deterministic case for a high value of the shock autocorrelation, so a negative correlation between growth and its variance will appear empirically. This shows the importance in applied work to separate expected volatility from unexpected volatility. Again we study how expected growth changes when the autocorrelation coefficient in the fiscal shock changes, while keeping its variance fixed. Note that again increasing the autocorrelation coefficient of the exogenous fiscal process has a non-linear effect on the average growth rate E(g).

We observe that the effect of uncertainty on consumption growth varies with the parameter η affecting the FELS. The lower the FELS, the higher the positive effect of a given amount of uncertainty upon growth. Finally, we notice that the relationship between expected growth, expected inflation and inflation variability is always positive, for a given level of persistence and a sufficiently high FELS. Again, as remarked under nominal wage setting, the sign of this relationship may become negative for high values of the persistence.

6 Concluding Remarks

In this paper we explore the links between short-run (cyclical) phenomena and long-run technological trend of output. The study of the issue has important policy implications as it opens the possibility that stabilization policies affect the long-run performance of the economy, with cumulative effects.

The impact of volatility on economic growth has been the subject of considerable investigation in the empirical literature. However, the evidence provided on the variability-growth relationship is mixed, with cross-section studies finding a negative correlation and time-series studies finding a positive correlation, especially when nominal volatility is jointly considered. Our results help in part to explain this evidence: in fact in the model presented the relationship between growth and volatility depends on the interplay of many factors, such as the source of the stochastic fluctuations in the economy, the functioning of the labour market, the elasticity of labour supply, the autocorrelation pattern of the shocks and the depreciation rate of capital.

We observe that in general growth is adversely affected by the volatility of the money supply shock, unless the Frisch elasticity of labour supply is low (but still consistent with available estimates). Conversely, the volatility of the technological shock has a positive impact on growth. Finally, the volatility of government spending will have a negative effect on growth for low enough values of the Frisch elasticity and/or for a high enough degree of serial correlation in the process governing the shocks.

Coming to the effect of the organization of the labour market, we show that money volatility will have a negative effect on growth only in the presence of nominal wage setting, while the effect of technology variability will be stronger and that of fiscal volatility weaker than with a competitive labour market.

We show that a higher rate of depreciation tends, *ceteris paribus*, to reinforce the negative effects of volatility on growth.

Our analysis provides a further step towards an understanding on the interconnection between short-run macroeconomic fluctuations and long-run growth. We are aware that more complex and realistic assumptions could be introduced as regards the conduct of fiscal and monetary policies, as well as the mechanisms driving growth and the sources of nominal rigidity. In this paper we have chosen to analyse a model which, though too complex to admit a closed form solution, was still simple enough to be interpreted behaviorally, and therefore serves the purpose of discovering new channels through which uncertainty impinges on growth. The insights obtained here prepare the ground for the development of a more general model whose internal workings are still understood, so that its implications for policy can be relied on: such development would provide a fruitful direction for future research.

Appendix

Derivation of (17): When $L_t = N_t$ using (10) we can rewrite (11) as: $W_t = \frac{(1-\beta)M_{t-1}\eta\lambda E_{t-1}L_t^{\eta}}{\alpha\mu E_{t-1}L_t a_t^{-1}}$, while, combining (3) and (10) we get $W_t = \alpha b_t L_t^{\alpha-1} K_t \frac{(1-\beta)\gamma M_t}{\mu C_t}$. Eliminating W_t from these two equations we get: $\frac{(1-\beta)M_{t-1}\eta\lambda E_{t-1}L_t^{\eta}}{\alpha\mu E_{t-1}L_t a_t^{-1}} = \alpha b_t L_t^{\alpha-1} K_t \frac{(1-\beta)\gamma M_t}{\mu C_t}$ which gives us (17) considering $M_t = a_t M_{t-1}$.

Derivation of (19): When $\delta = 100\%$ we have: $K_{t+2} + C_{t+1} + G_{t+1} = Y_{t+1} = K_{t+1}(1+R_{t+1})(1-\alpha)^{-1}$, where the second equality comes from (4). We can then write (8) as:

$$C_t^{-1}K_{t+1} = \beta E_t C_{t+1}^{-1} (K_{t+2} + C_{t+1} + G_{t+1})(1 - \alpha). \tag{41}$$

When u_t is i.i.d. (and uncorrelated with each other) we can write $E_t u_{t+i} \equiv u$ for all i = 1, 2..n. Iterating and considering the transversality condition we then have:

$$C_t = \frac{1 - \varkappa}{\varkappa (1 + u)} K_{t+1},\tag{42}$$

where $\varkappa \equiv \alpha(1-\beta)$. Using: $C_t(1+u_t) + K_{t+1} = Y_t$ we can easily derive (19) and:

$$C_t = \frac{1 - \varkappa}{(1 + u_t)(1 - \varkappa) + \varkappa(1 + u)} Y_t. \tag{43}$$

Derivation of (20): Combining (10) and (43) we have:

$$M_t(1-\beta)\mu^{-1} = \frac{(1-\varkappa)}{\gamma [(1+u_t)(1-\varkappa) + \varkappa(1+u)]} Y_t P_t.$$

Using (3) and rearranging we have:

$$L_t = \frac{\alpha \gamma M_t (1 - \beta) \left[(1 + u_t)(1 - \varkappa) + \varkappa (1 + u) \right]}{\mu (1 - \varkappa) W_t}.$$
 (44)

We can then compute:

$$\eta \lambda L_t^{\eta} = \eta \lambda \left(\frac{\gamma \varkappa M_t \left[(1 + u_t)(1 - \varkappa) + \varkappa (1 + u) \right]}{\mu (1 - \varkappa) W_t} \right)^{\eta},$$

and

$$\eta \lambda E_{t-1} L_t^{\eta} = \eta \lambda E_{t-1} \left(\frac{M_t \varkappa \left[(1 + u_t)(1 - \varkappa)\gamma_t + \varkappa \gamma(1 + u) \right]}{\mu(1 - \varkappa)W_t} \right)^{\eta}. \tag{45}$$

Using (43), (11) can be rewritten as:

$$\eta \lambda E_{t-1} L_t^{\eta} = \alpha E_{t-1} W_t L_t (Y_t P_t)^{-1} (1 - \varkappa)^{-1} \gamma \left[(1 + u_t (1 - \varkappa) + \varkappa (1 + u)) \right]
= \frac{\alpha^2}{1 - a} \gamma E_{t-1} \left[(1 + u_t (1 - \varkappa) \gamma + \varkappa (1 + u)) \right].$$

The second equality is obtained using (3). Finally, using the assumed properties of the distribution of the shock u_t we have $\eta \lambda E_{t-1} L_t^{\eta} = \frac{\alpha^2 \gamma (1+u)}{1-\varkappa}$, using which in (45) we arrive to:

$$W_t^{\eta} \frac{\alpha^2 \gamma(1+u)}{1-\varkappa} = \eta \lambda E_{t-1} \left(\frac{\gamma M_t \varkappa \left[(1+u_t)(1-\varkappa) + \varkappa(1+u) \right]}{\mu(1-\varkappa)} \right)^{\eta}.$$

To proceed further we assume $\eta=1.^{10}$ Assuming $\rho_a=0$ and $\rho_\lambda=0$, the expression above becomes:

$$W_t = \frac{M_{t-1} \varkappa \lambda a}{\alpha^2 \mu}.$$

This, using (44), can be rewritten as (20).

Derivation of (23): If we combine (43) and (12), while considering that labour income is α times total income, we get (23).

 $^{^{10}\}mathrm{Another}$ possibility, pursued in Blackburn and Pelloni (2005) is to treat u_t as constant through time.

Proof of Proposition 1: From the economy wide resource constraint we have:

$$K_{t+1} = Y_t - C_t(1+u_t) = b_t K_t L_t^{\alpha} - C_t(1+u_t) = b_t K_t L_t^{\alpha} - \frac{(1+u_t)(1-\varkappa)}{\varkappa(1+u)} K_{t+1},$$

where the second equality comes by using the production function and the third by recalling (42). We can then write:

$$\frac{K_{t+1}}{K_t} = \frac{b_t L_t^{\alpha}}{1 + \frac{(1+u_t)(1-\varkappa)}{\varkappa(1+u)}}.$$
(46)

Plugging (20) in this and rearranging we get:

$$\frac{K_{t+1}}{K_t} = \frac{b_t \left(\frac{\alpha^2 a_t [(1-\varkappa)(1+u_t)+\varkappa(1+u)]}{a\lambda(1-\varkappa)}\right)^{\alpha}}{\frac{\varkappa(1+u)+(1+u_t)(1-\varkappa)}{\varkappa(1+u)}} = \frac{b_t \varkappa(1+u) \left(\frac{\alpha^2 a_t}{a\lambda(1-\varkappa)}\right)^{\alpha}}{[(1-\varkappa)(1+u_t)+\varkappa(1+u)]^{\alpha-1}}.$$

By (42), this is also equal to: $\frac{C_t}{C_{t-1}}$, so that the expression for $\frac{C_{t+1}}{C_t} - 1$ in (21) holds.

Proof of Proposition 2: Substituting (23) in (46) we have:

$$\frac{K_{t+1}}{K_t} = \frac{b_t \left(\frac{\alpha[(1-\varkappa)(1+u_t)+\varkappa(1+u)]}{\eta\lambda(1-\varkappa)}\right)^{\alpha/\eta}}{1 + \frac{(1+u_t)(1-\varkappa)}{\varkappa(1+u)}}.$$

By (42), this is also equal to: $\frac{C_t}{C_{t-1}}$, so that the expression for $\frac{C_{t+1}}{C_t} - 1$ in (24) holds.

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Table 1: Baseline Calibration

Para	meters	
β	0.96	Subjective discount factor
δ	0.1	Depreciation rate
α	0.7	Cost share of labour
η	2.5	Preference parameter
$ ho_a$	0.69	Autoregressive parameter in the monetary shock
$ ho_b$	0.85	Autoregressive parameter in the technology shock
$ ho_u$	0.87	Autoregressive parameter in the fiscal shock
$\sigma_{arepsilon_a}$	0.0190	Standard deviation of the innovation ε_a
$\sigma_{arepsilon_b}$	0.0212	Standard deviation of the innovation ε_b
$\sigma_{arepsilon_u}$	0.0102	Standard deviation of the innovation ε_u
Rati	os over (Capital and Steady-State Values
$\overline{m_p}$	0.26	Real money balances
s	0.1	Government spending
π	4%	Inflation
L	0.2	Labour supply
g	2%	Consumption growth rate

Table 2: Volatility of the Monetary Shock under Nominal Wage Setting

Benchmark	σ_{ε_a}	ρ_a	σ_a	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	0.019	0.69	0.0263	1.9968	$0.9\overline{2}22$	0.1999	0.0061	3.9935	1.9256
The effect of σ_{ε_a}	σ_{ε_a}	ρ_a	σ_a	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	0.01	0.69	0.0138	1.9991	0.4854	0.2000	0.0032	3.9982	1.0135
	0.03	0.69	0.0415	1.9921	1.4561	0.1997	0.0097	3.9837	3.0405
	0.05	0.69	0.0691	1.9781	2.4269	0.1991	0.0162	3.9548	5.0675
	0.08	0.69	0.1105	1.9439	3.8830	0.1977	0.0259	3.8842	8.1080
	0.10	0.69	0.1382	1.9122	4.8538	0.1964	0.0324	3.8190	10.1350
	0.15	0.69	0.2072	1.8025	7.2807	0.1919	0.0485	3.5928	15.2024
The effect of ρ_a	$\sigma_{arepsilon_a}$	ρ_a	σ_a	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	0.019	0	0.0190	1.9949	0.8504	0.1998	0.0064	3.9969	0.9956
	0.019	0.50	0.0219	1.9961	0.8921	0.1999	0.0062	3.9951	1.3977
	0.019	0.90	0.0436	1.9969	0.9843	0.1998	0.0065	3.9886	3.7698
The effect of ρ_a	$\sigma_{arepsilon_a}$	ρ_a	σ_a	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
given σ_a	0.0263	0	0.0263	1.9903	1.1750	0.1997	0.0088	3.9929	1.6724
	0.0227	0.50	0.0263	1.9945	1.0673	0.1998	0.0074	3.9941	1.3755
	0.0114	0.90	0.0263	1.9989	0.5928	0.1999	0.0039	3.9958	2.2702
The effect of η				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	$\eta = 1.5$			2.0037	0.9903	0.2000	0.0063	3.9854	1.8300
	$\eta = 3.5$			1.9908	0.8987	0.1998	0.0062	4.0000	1.9606
	$\eta = 4.5$			1.9850	0.8867	0.1997	0.0062	4.0061	1.9787
	$\eta = 6$			1.9766	0.8768	0.1995	0.0062	4.0150	1.9939
Sensitivity				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	$\beta = 0.9$			1.9967	0.9411	0.1999	0.0060	3.9935	1.9118
	$\beta = 0.9$			1.9969	0.9073	0.1999	0.0062	3.9934	1.9364
	$\delta = 0.0$			1.9968	0.8676	0.1998	0.0065	3.9937	1.9634
	$\delta = 0.1$			1.9967	0.9667	0.1999	0.0059	3.9934	1.8938
	$\delta = 0.1$			1.9965	1.0038	0.1999	0.0056	3.9934	1.8661
	L = 0.1			1.9968	0.9222	0.1699	0.0052	3.9935	1.9256
	L=0.3	3		1.9968	0.9222	0.2998	0.0092	3.9935	1.9256
	$\pi = 0$			1.9966	0.9576	0.1999	0.0064	-0.0069	1.9277
	$\pi = 0.0$			1.9967	0.9396	0.1999	0.0063	1.9933	1.9267
	$\pi = 0.0$			1.9969	0.9055	0.1999	0.0060	5.9936	1.9246
	$\pi = 0.0$	18		1.9970	0.8895	0.1999	0.0059	7.9938	1.9235

Table 3: Volatility of the Technology Shock under Nominal Wage Setting

Table 3: Volatility of the Technology Shock under Nominal Wage Setting									
Benchmark	σ_{ε_b}	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	0.0212	0.85	0.0402	2.0104	1.1790	0.2000	0.0013	4.0033	1.2021
The effect of σ_{ε_h}	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
Ü	0.01	0.85	0.0190	2.0023	0.5561	0.2000	0.0006	4.0007	0.5670
	0.04	0.85	0.0759	2.0369	2.2245	0.2000	0.0024	4.0119	2.2681
	0.06	0.85	0.1139	2.0830	3.3368	0.1999	0.0037	4.0267	3.4022
	0.08	0.85	0.1519	2.1476	4.4490	0.1999	0.0049	4.0474	4.5363
	0.10	0.85	0.1898	2.2306	5.5613	0.1998	0.0061	4.0741	5.6703
	0.15	0.85	0.2847	2.5187	8.3419	0.1995	0.0092	4.1667	8.5055
The effect of ρ_b	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	0.0212	0	0.0212	2.0043	0.8696	0.2000	0.0029	4.0032	0.8867
	0.0212	0.10	0.0213	2.0046	0.8842	0.2000	0.0028	4.0031	0.9016
	0.0212	0.30	0.0222	2.0054	0.9224	0.2000	0.0025	4.0030	0.9405
	0.0212	0.50	0.0245	2.0066	0.9781	0.2000	0.0022	4.0029	0.9973
	0.0212	0.70	0.0297	2.0083	1.0654	0.2000	0.0018	4.0029	1.0863
	0.0212	0.95	0.0679	2.0124	1.3626	0.2000	0.0009	4.0059	1.3893
	0.0212	0.99	0.1503	2.0135	1.8990	0.1999	0.0008	4.0223	1.9362
The effect of ρ_b	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
given σ_b	0.0402	0	0.0402	2.0156	1.6508	0.1999	0.0054	4.0114	1.6832
	0.0400	0.10	0.0402	2.0165	1.6701	0.1999	0.0052	4.0110	1.7029
	0.0384	0.30	0.0402	2.0178	1.6704	0.1999	0.0046	4.0098	1.7032
	0.0369	0.40	0.0402	2.0180	1.6485	0.1999	0.0042	4.0088	1.6808
	0.0349	0.50	0.0402	2.0177	1.6080	0.1999	0.0037	4.0078	1.6395
	0.0287	0.70	0.0402	2.0153	1.4443	0.2000	0.0024	4.0053	1.4726
	0.0175	0.90	0.0402	2.0077	1.0286	0.2000	0.0010	4.0027	1.0488
	0.0057	0.99	0.0402	2.0010	0.5085	0.2000	0.0003	4.0016	0.5185
The effect of η				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	$\eta = 1.5$			2.0112	1.2008	0.2000	0.0014	4.0030	1.2244
	$\eta = 3.5$			2.0099	1.1705	0.2000	0.0013	4.0036	1.1934
	$\eta = 4.5$			2.0096	1.1660	0.2000	0.0013	4.0038	1.1888
	$\eta = 6$			2.0091	1.1620	0.2000	0.0013	4.0042	1.1848
Sensitivity				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	$\beta = 0.9$	5		2.0088	1.1040	0.2000	0.0012	4.0032	1.1256
	$\beta = 0.9$	7		2.0117	1.2403	0.2000	0.0014	4.0035	1.2647
	$\delta = 0.0$	75		2.0138	1.3362	0.2000	0.0018	4.0037	1.3624
	$\delta = 0.12$	25		2.0080	1.0574	0.2000	0.0009	4.0030	1.0781
	$\delta = 0.18$	5		2.0063	0.9609	0.2000	0.0007	4.0028	0.9797
	L = 0.1	7		2.0082	1.0522	0.1700	0.0010	4.0027	1.0728
	L = 0.3	}		2.0183	1.5659	0.3000	0.0026	4.0059	1.5966

Table 4: Volatility of the Fiscal Shock under Nominal Wage Setting

Table 4: Volatility of the Fiscal Shock under Nominal Wage Setting										
Benchmark	σ_{ε_u}	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.0102	0.87	0.0206	2.0000	0.2889	0.2000	0.0021	4.0008	0.2946	
The effect of σ_{ε_u}	$\sigma_{arepsilon_u}$	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.005	0.87	0.0101	2.0000	0.1420	0.2000	0.0010	4.0002	0.1448	
	0.03	0.87	0.0608	2.0002	0.8519	0.1998	0.0061	4.0070	0.8686	
	0.05	0.87	0.1014	2.0007	1.4198	0.1996	0.0101	4.0194	1.4476	
	0.07	0.87	0.1420	2.0014	1.9877	0.1992	0.0142	4.0381	2.0267	
	0.10	0.87	0.2028	2.0028	2.8400	0.1984	0.0203	4.0777	2.8952	
	0.125	0.87	0.2535	2.0044	3.5494	0.1976	0.0254	4.1215	3.6190	
The effect of ρ_u	$\sigma_{arepsilon_u}$	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.0102	0	0.0102	2.0000	0.1221	0.2000	0.0008	4.0001	0.1245	
	0.0102	0.10	0.0102	2.0000	0.1306	0.2000	0.0008	4.0001	0.1332	
	0.0102	0.30	0.0107	2.0001	0.1521	0.2000	0.0010	4.0002	0.1551	
	0.0102	0.50	0.0117	2.0001	0.1820	0.2000	0.0012	4.0002	0.1856	
	0.0102	0.70	0.0142	2.0001	0.2269	0.2000	0.0015	4.0004	0.2314	
	0.0102	0.95	0.0326	1.9995	0.3383	0.2000	0.0028	4.0016	0.3449	
	0.0102	0.99	0.0721	1.9958	0.4212	0.1999	0.0049	4.0060	0.4295	
The effect of ρ_u	$\sigma_{arepsilon_u}$	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
given σ_u	0.0206	0	0.0206	2.0003	0.2476	0.2000	0.0016	4.0003	0.2524	
	0.0205	0.10	0.0206	2.0004	0.2632	0.2000	0.0017	4.0003	0.2683	
	0.0197	0.30	0.0206	2.0005	0.2925	0.2000	0.0019	4.0004	0.2982	
	0.0179	0.50	0.0206	2.0005	0.3160	0.2000	0.0021	4.0005	0.3223	
	0.0165	0.60	0.0206	2.0005	0.3229	0.2000	0.0022	4.0005	0.3292	
	0.0147	0.70	0.0206	2.0004	0.3226	0.2000	0.0022	4.0005	0.3290	
	0.0124	0.80	0.0206	2.0003	0.3086	0.2000	0.0022	4.0006	0.3146	
	0.0090	0.90	0.0206	2.0001	0.2630	0.2000	0.0021	4.0006	0.2681	
	0.0064	0.95	0.0206	1.9999	0.2113	0.2000	0.0019	4.0006	0.2154	
The effect of η				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	$\eta = 1.5$			2.0003	0.2721	0.2000	0.0023	4.0004	0.2774	
	$\eta = 3.5$			1.9996	0.2972	0.2000	0.0020	4.0013	0.3030	
	$\eta = 4.5$			1.9991	0.3020	0.2000	0.0020	4.0019	0.3079	
	$\eta = 6$			1.9982	0.3063	0.1999	0.0020	4.0027	0.3123	
Sensitivity				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	$\beta = 0.9$	5		2.0000	0.2998	0.2000	0.0021	4.0009	0.3057	
	$\beta = 0.9$	7		2.0001	0.2795	0.2000	0.0020	4.0007	0.2850	
	$\delta = 0.0$	75		2.0001	0.2770	0.2000	0.0020	4.0006	0.2824	
	$\delta = 0.12$	25		1.9999	0.2972	0.2000	0.0021	4.0010	0.3031	
	$\delta = 0.18$	5		1.9997	0.3035	0.2000	0.0022	4.0012	0.3094	
	L = 0.1	7		2.0000	0.2889	0.1700	0.0018	4.0008	0.2946	
	L = 0.3	1		2.0000	0.2889	0.3000	0.0031	4.0008	0.2946	

Table 5: Volatility of the Technology Shock under Competitive Labour Market

Table 5: Volatility of the Technology Shock under Competitive Labour Market										
Benchmark	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.0212	0.85	0.0402	2.008	1.0698	0.2000	0.0006	4.0028	1.0908	
The effect of σ_{ε_b}	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.01	0.85	0.0190	2.0019	0.5046	0.2000	0.0003	4.0006	0.5145	
	0.04	0.85	0.0759	2.0300	2.0185	0.2000	0.0012	4.0101	2.0581	
	0.06	0.85	0.1139	2.0676	3.0278	0.2000	0.0017	4.0227	3.0871	
	0.08	0.85	0.1519	2.1202	4.0370	0.1999	0.0023	4.0403	4.1162	
	0.10	0.85	0.1898	2.1878	5.0463	0.1999	0.0029	4.0630	5.1452	
	0.15	0.85	0.2847	2.4226	7.5694	0.1998	0.0043	4.1418	7.7179	
The effect of ρ_b	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	0.0212	0	0.0212	2.0024	0.5920	0.2000	0.0008	4.0010	0.6036	
	0.0212	0.10	0.0213	2.0026	0.6158	0.2000	0.0008	4.0011	0.6279	
	0.0212	0.30	0.0222	2.0032	0.6775	0.2000	0.0007	4.0013	0.6908	
	0.0212	0.50	0.0245	2.0043	0.7660	0.2000	0.0007	4.0015	0.7810	
	0.0212	0.70	0.0297	2.0060	0.9016	0.2000	0.0007	4.0020	0.9193	
	0.0212	0.95	0.0679	2.0111	1.3063	0.2000	0.0006	4.0057	1.3319	
	0.0212	0.99	0.1503	2.0127	1.8741	0.1999	0.0008	4.0222	1.9109	
The effect of ρ_b	$\sigma_{arepsilon_b}$	ρ_b	σ_b	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
given σ_b	0.0402	0	0.0402	2.0087	1.1238	0.2000	0.0015	4.0038	1.1458	
	0.0400	0.1	0.0402	2.0094	1.1631	0.2000	0.0014	4.0039	1.1859	
	0.0384	0.3	0.0402	2.0107	1.2269	0.2000	0.0013	4.0042	1.2510	
	0.0349	0.5	0.0402	2.0115	1.2593	0.2000	0.0011	4.0041	1.2840	
	0.0287	0.7	0.0402	2.0111	1.2223	0.2000	0.0009	4.0036	1.2463	
	0.0266	0.75	0.0402	2.0106	1.1905	0.2000	0.0008	4.0034	1.2139	
	0.0175	0.9	0.0402	2.0066	0.9582	0.2000	0.0005	4.0025	0.9770	
	0.0057	0.99	0.0402	2.0009	0.5019	0.2000	0.0002	4.0016	0.5117	
The effect of η				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	$\eta = 1.5$			2.0099	1.1365	0.2000	0.0011	4.0028	1.1588	
	$\eta = 3.5$			2.0079	1.0436	0.2000	0.0004	4.0028	1.0640	
	$\eta = 4.5$			2.0076	1.0295	0.2000	0.0003	4.0028	1.0497	
	$\eta = 6$			2.0074	1.0176	0.2000	0.0002	4.0029	1.0375	
Sensitivity				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$	
	$\beta = 0.9$	5		2.0072	1.0032	0.2000	0.0006	4.0027	1.0228	
	$\beta = 0.9$	7		2.0095	1.1244	0.2000	0.0007	4.0029	1.1465	
	$\delta = 0.0$	75		2.0111	1.1950	0.2000	0.0008	4.0030	1.2184	
	$\delta = 0.12$	25		2.0066	0.9712	0.2000	0.0005	4.0027	0.9903	
	$\delta = 0.1$	5		2.0053	0.8918	0.2000	0.0004	4.0026	0.9093	
	L = 0.1	7		2.0067	0.9548	0.1700	0.0005	4.0023	0.9735	
	L = 0.3			2.0149	1.4209	0.3000	0.0012	4.0050	1.4488	

Table 6: Volatility of the Fiscal Shock under Competitive Labour Market

Benchmark				E(g)%	$\frac{\sigma_g\%}{\sigma_g\%}$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
Denominar k	σ_{ε_u} 0.010	$ \rho_u $ 0.87	σ_u 0.0206	2.0020	0.4678	0.2000	0.0010	4.0002	0.4770
The effect of -				E(g)%	$\sigma_g\%$	E(L)		$E(\pi)\%$	$\sigma_{\pi}\%$
The effect of $\sigma_{\varepsilon u}$	$\sigma_{arepsilon_u} \ 0.005$	$ \rho_u $ 0.87	σ_u 0.0101	$\frac{E(g)}{2.0005}$	0.2299	0.2000	σ_L 0.0005	4.0000	0.2344
	0.003	0.87	0.0608	2.0003 2.0172	1.3795	0.2000	0.0030	4.0013	1.4065
	0.05	0.87	0.1014	2.0482	2.2992	0.2000 0.1999	0.0050	4.0013 4.0037	2.3442
	0.03 0.07	0.87	0.1014 0.1420	2.0462 2.0945	3.2189	0.1998	0.0030 0.0071	4.0037 4.0072	3.2819
	0.10	0.87	0.1420 0.2028	2.1929	4.5983	0.1996	0.0071	4.0072 4.0147	4.6885
	0.10 0.125	0.87	0.2525 0.2535	2.3014	5.7479	0.1990 0.1994	0.0101 0.0126	4.0147 4.0229	5.8606
				l .					
The effect of ρ_u	$\sigma_{arepsilon_u} \ 0.010$	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
		0	0.0102	2.0004	0.1994	0.2000	0.0002	4.0000	0.2033
	0.010	0.10	0.0102	2.0004	0.2134	0.2000	0.0002	4.0000	0.2176
	0.010	0.30	0.0107	2.0006	0.2484	0.2000	0.0003	4.0000	0.2533
	0.010	0.50	0.0117	2.0009	0.2971	0.2000	0.0004	4.0000	0.3029
	0.010	0.70	0.0142	2.0013	0.3698	0.2000	0.0006	4.0000	0.3770
	0.010	0.95	0.0326	2.0021	0.5388	0.2000	0.0018	4.0008	0.5494
	0.010	0.97	0.0419	2.0017	0.5645	0.2000	0.0025	4.0015	0.5756
	0.010	0.98	0.0511	2.0010	0.5828	0.2000	0.0031	4.0024	0.5942
	0.010	0.99	0.0721	1.9988	0.6171	0.1999	0.0044	4.0051	0.6292
The effect of ρ_u	σ_{ε_u}	ρ_u	σ_u	E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
given σ_u	0.0206	0.10	0.0206	2.0019	0.4307	0.2000	0.0005	3.9999	0.4392
	0.0197	0.30	0.0206	2.0023	0.4806	0.2000	0.0005	3.9999	0.4900
	0.0179	0.50	0.0206	2.0027	0.5218	0.2000	0.0006	3.9999	0.5321
	0.0165	0.60	0.0206	2.0028	0.5345	0.2000	0.0007	4.0000	0.5450
	0.0147	0.70	0.0206	2.0028	0.5356	0.2000	0.0008	4.0000	0.5461
	0.0090	0.90	0.0206	2.0016	0.4344	0.2000	0.0011	4.0002	0.4429
	0.0064	0.95	0.0206	2.0008	0.3412	0.2000	0.0012	4.0003	0.3479
The effect of η				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_\pi\%$
	$\eta = 1.5$			2.0011	0.3742	0.2000	0.0018	4.0002	0.3816
	$\eta = 3.5$			2.0024	0.5064	0.2000	0.0007	4.0001	0.5164
	$\eta = 4.5$			2.0026	0.5274	0.2000	0.0005	4.0001	0.5377
	$\eta = 6$			2.0028	0.5454	0.2000	0.0004	4.0001	0.5561
Sensitivity				E(g)%	$\sigma_g\%$	E(L)	σ_L	$E(\pi)\%$	$\sigma_{\pi}\%$
	$\beta = 0.9$			2.0022	0.4926	2.0022	0.4926	4.0002	0.5022
	$\beta = 0.9$			2.0018	0.4475	0.2000	0.0010	4.0001	0.4563
	$\delta = 0.0$			2.0017	0.4315	0.2000	0.0009	4.0001	0.4399
	$\delta = 0.12$			2.0022	0.4969	0.2000	0.0011	4.0002	0.5067
	$\delta = 0.1$			2.0013	0.2331	0.2000	0.0011	4.0003	0.5311
	L = 0.1			2.0020	0.4678	0.1700	0.0009	4.0002	0.4770
	L = 0.3	}		2.0020	0.4678	0.3000	0.0015	4.0002	0.4770





